

MINISTRY OF EDUCATION AND SCIENCE OF UKRAINE  
V. N. KARAZIN KHARKIV NATIONAL UNIVERSITY

**MEDICAL AND BIOLOGICAL PHYSICS.**  
**Practicum for students studying the subject in English**

Kharkiv – 2018

УДК 577.3 + 577.115 + 543.9 (076.6)

M 46

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The material contained in the practicum represents the basic theoretical framework of medical and biological physics. Each chapter provides a short description of the theoretical material, the typical problems and formulas required for the problem solution. The examples of solved problems are presented at the end of the subsections. The practicum is intended for students studying the medical and biological physics in English.

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